

New Spins on the WGC



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with Gary Shiu



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Landscape vs. Swampland

In order to distinguish the **landscape** from the **swampland**, various swampland conjectures have been proposed. [\[cf. many talks\]](#)

Typically, these conjectures can be **formulated** and **tested** by going to **extreme regions** of parameter space.

In the swampland/landscape, **black holes** play a central role. Charged/rotating BHs have an **extremal limit**: $T \rightarrow 0$.



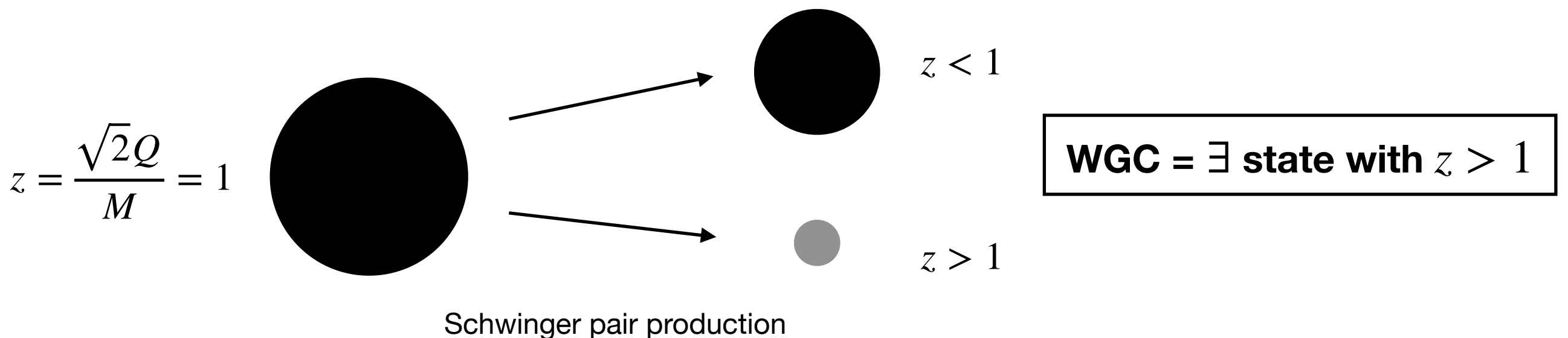
**What lessons about the swampland
can we learn from extremal BHs?**

Weak Gravity Conjecture

The WGC suggests that **extremal black holes**, unless protected by symmetry, should be **unstable**.

Instability seems to be a key property of the **landscape** (e.g. AdS instability conjecture, no dS conjecture..)

For charged black holes, this puts a **bound on the spectrum**.



Mild Form of the WGC

The WGC constrains **higher-derivative corrections** to Einstein-Maxwell, as they modify the extremality bound. [Arkani-Hamed, Motl, Nicolis, Vafa '06] [Kats, Motl, Padi '06]

Leading Corrections:
$$L = \frac{1}{2}R - \frac{1}{4}F_{ab}F^{ab} + \frac{a_1}{4}(F_{ab}F^{ab})^2 + \frac{a_2}{2}F_{ab}F_{cd}W^{abcd}$$

Extremality Bound:
$$\frac{\sqrt{2}Q}{M} \leq 1 + \frac{32\pi^2(2a_1 - a_2)}{Q^2}$$

The WGC requires:
$$2a_1 - a_2 \geq 0$$

Black hole instability constrains EFTs!

Rotating Black Holes

Can we get **new constraints** by studying different extremal black holes?

What about **extremal rotating** black holes?

This amounts to a "**rotating WGC**", but its current status is unclear.

Evidence

c-theorem for BTZ

[LA, Cole, Loges, Shiu '20]

Causality for higher spins

[Kaplan, Kundu '21]

Counter Evidence

Superradiance

Ultraspinning regime

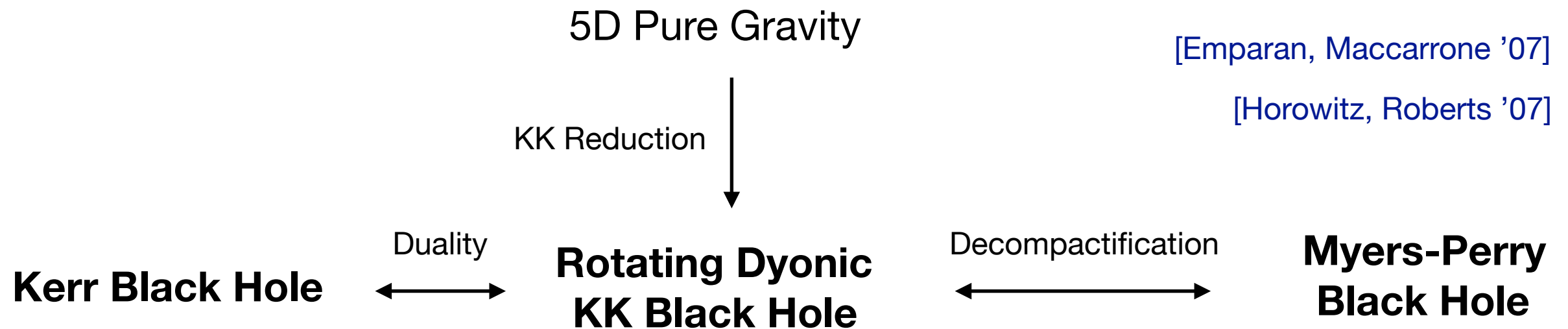
in $D > 5$

[Myers, Perry '86]

In string theory, we can make use of duality chains to map **charge** to **rotation** and vice versa.

Mapping Rotation to Charge

To assess the status of the rotating WGC, we can map **rotating** to **charged black holes**.



We can **impose the WGC** on non-rotating, charged KK black holes.

This will tell us how the charged WGC bounds **higher-derivative corrections** to rotating black holes.

Correction to MP Black Hole

[LA, Shiu '22]

The black holes of interest are **5D vacuum solutions**. The leading corrections are given by:

$$L = R + \lambda(\text{Riem})^2 + \eta(\text{Riem})^3$$

Keeping angular momentum fixed, the **mass correction** is:

$$\delta M_{\text{MP}} = -4\pi^2\lambda \left(\frac{a^2 + b^2 - 6|ab|}{|ab|} \right) - 16\pi^2\eta \left(\frac{(a^2 - 14|ab| + b^2)(a^2 - |ab| + b^2)}{7|ab|^3} \right)$$

$$(a, b) \sim (J_1, J_2)$$

For arbitrary ratio of rotations **a/b** , the sign of the correction is **not fixed!** No rotating WGC?

Leading Corrections

[LA, Shiu '22]

However, for arbitrary 5D rotation the 4D KK BH is not purely charged.

In the limit of equal 5D rotations, $J_1 - J_2 = 0$, the 4D KK BH contains **just charge**. The corrections are then:

5D Myers-Perry:
$$\delta M_{\text{MP}} \Big|_{a \pm b = 0} = 16\pi^2 \lambda + \frac{192\pi^2}{7a^2} \eta$$

4D Kaluza-Klein:
$$\delta M_{\text{KK}} = -\lambda M_\lambda(q/p) + \eta M_\eta(q/p) \quad M_i \geq 0$$

4D Kerr:
$$\delta M_{\text{Kerr}} = \frac{8\pi\eta}{7\alpha^3}$$

Imposing the WGC

[LA, Shiu '22]

We now have computed all corrections and can **impose the WGC** on the 4D charged black hole.

	$\frac{\lambda}{L}\mathcal{R}^2$	$\eta L\mathcal{R}^3$
δM_4^{KK}	$-\frac{\lambda}{L}\mathcal{M}_\lambda$	$\eta L\mathcal{M}_\eta$
WGC:	$\lambda \geq 0$	$\eta \leq 0$
δM_5^{MP}	$\frac{\lambda}{L}16\pi^2$	$\eta L\frac{192\pi^2}{7a^2}$
Sign:	+	-
δM_4^{Kerr}	0	$\eta L\frac{8\pi}{7\hat{\alpha}^3}$
Sign:	n.a.	-

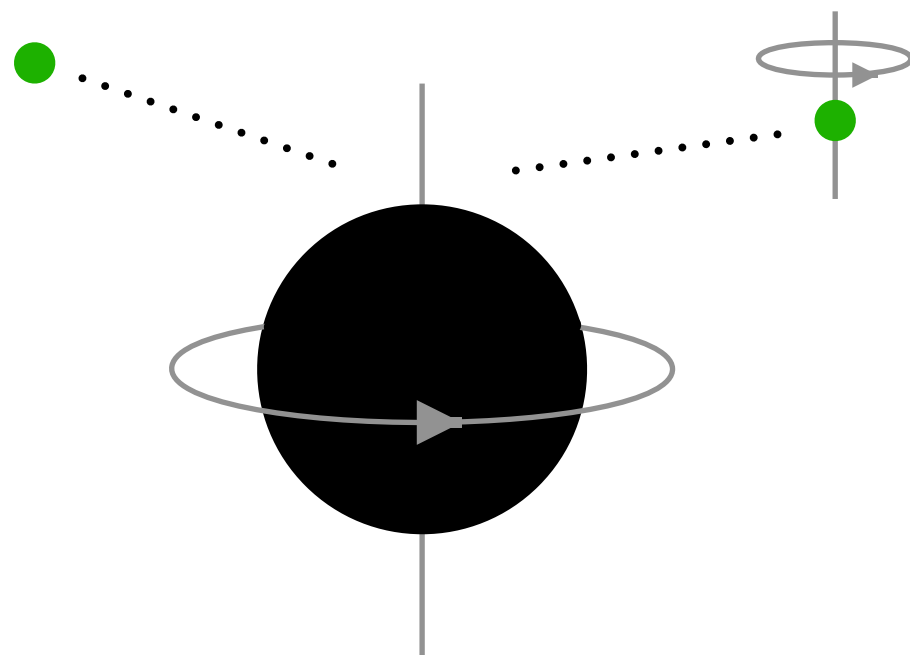
Riem² term **increases** the mass of MP.

Riem³ **decreases** the mass of MP and Kerr.

Superradiance

The charged WGC constrains rotating black holes, but a rotating WGC only holds on a **case-by-case basis**.

An interpretation of this is that, typically, extremal rotating black holes have a **superradiant instability**.



No WGC-like constraint on spectrum!

Only **non-superradiant extremal black holes** should obey additional constraints. BTZ is an example? [\[Ortíz '11\]](#)

Conclusions

Extremal black holes can help us distinguish the landscape from the swampland.

Instability places **constraints on EFTs**, in particular Wilson coefficients of higher-dimensional operators.

Assuming the WGC, we derived **new constraints on rotating BHs** by mapping rotation to charge.

Superradiance prevents a universal rotating WGC-like constraint.

Interesting to study rotating solutions that don't superradiate.

Thank you!

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